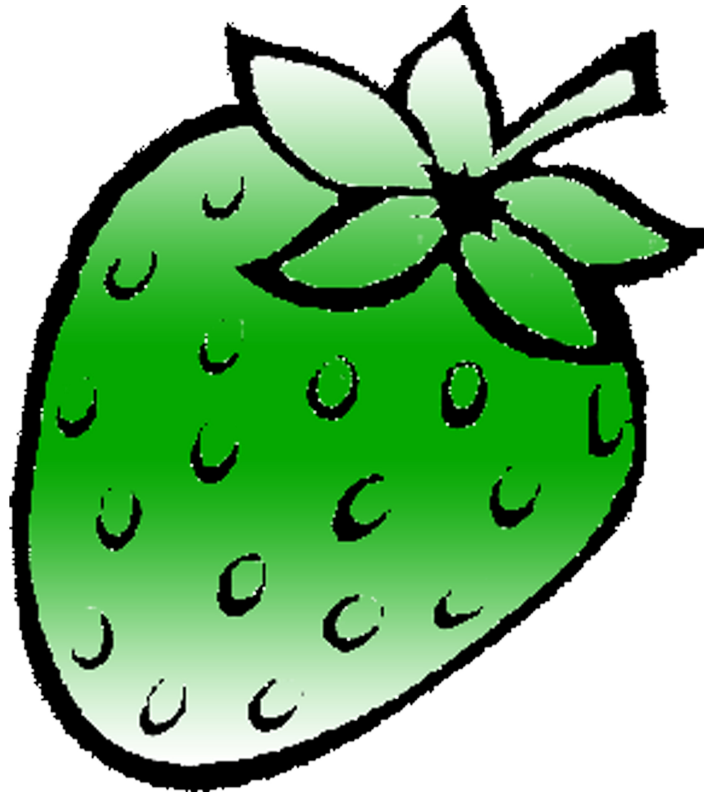


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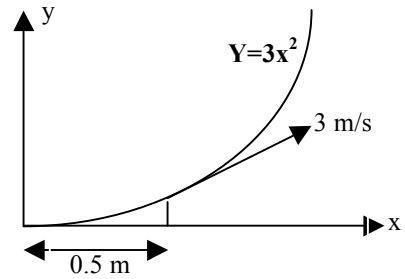
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KINEMATICS OF PARTICLES

1. The angular acceleration of a flywheel of diameter 0.6 m, rotating about its centroidal axis is given by $\alpha = \theta/4 \text{ rad/s}^2$ where θ is in radians. Determine the magnitude of the velocity and magnitude of resultant acceleration of a point on the rim of the flywheel at $\theta = 2$ radians.
 Ans. : assuming at $\theta = 0, \omega = 0, v = 0.3 \text{ m/s}, a = 0.335 \text{ m/s}^2$
2. A particle moves in the x-y plane with acceleration components $a_x = -3 \text{ m/s}^2$ and $a_y = -16 \text{ m/s}^2$. If its initial velocity is $v_0 = 50 \text{ m/s}$ directed at 30° to the axis compute the radius of curvature of the path at $t=2$ seconds.
 Hint : $1/\rho = (V_x a_y - V_y a_x) / ((V_x^2 + V_y^2)^{3/2})$
 Ans. : 88.47 m
3. A train starts from rest on a curved path of radius 800m. Its speed increases uniformly and after 3 minutes it is 72km/hr. Find the tangential, normal and total accelerations after 2 minutes.
 Ans. : $a_t = 1/9 \text{ m/s}^2, a_n = 2/9 \text{ m/s}^2$
4. A car starts from rest at $t = 0$ along a circular track of radius 200m. The rate of increase in speed of the car is uniform. At the end of 60 sec. The speed of the car is 24km/hr. Find the normal and tangential components of acceleration at time $t = 30$ sec.
 Ans. : $a_t = 1/9 \text{ m/s}^2, a_n = 1/18 \text{ m/s}^2$
5. A particle moves along a circle of radius 20 cm so that $S = 20\pi t^2$ cm. Find its tangential and normal accelerations after it has completed a revolution.
 Ans. : $a_t = 40 \pi \text{ cm/sec}^2, a_n = 160 \pi^2 \text{ cm/sec}^2$
6. A particle moves according to the equation $r(t) = 50 \cos 4t^2 \mathbf{i} + 50 \sin 4t^2 \mathbf{j}$ where distance are in cm and the time in sec. Find its velocity, tangential and normal accelerations.
 Ans. : $v = 400 \text{ cm/s}^2, a_t = 400, a_n = 3200 t^2 \text{ cm/sec}^2$
7. The motion of a particles is defined by a relation- $r(t) = 30 \sin(2t^2) \mathbf{i} + 30 \cos(2t^2) \mathbf{j}$ Find the velocity, tangential and normal components of accelerations at time $t = 3$ sec.
8. A car travels along a depression in a road, the equation of the depression being $x^2 = 200y$. The speed of the car is constant and equal to 72 Km/hour. Find its acceleration when the car is at the deepest point in the depression. What is the radius of curvature of the depression at this point?
 Ans. : $\rho = 100\text{m}, a = a_n = 4 \text{ m/sec}^2$
9. The movement of a particle is defined by $r(t) = t \mathbf{i} + t^2 \mathbf{j}$ where t is in sec and distances in m. Find the minimum radius of curvature of the path and the velocity and acceleration at this point. (T)
 Ans. : $v = 1 \text{ m/sec}, a_n = 2 \text{ m/sec}^2, \rho = 0.5 \text{ m}$
10. Particle moves in a plane with constant acceleration $a = 2 \mathbf{i} \text{ m/s}^2$. At $t = 0$ the velocity of the particle was $V_0 = \mathbf{i} + 1.732 \mathbf{j} \text{ m/s}$. Find the radius of curvature of its path at $t = 1$ sec and the tangential and normal components of the acceleration. (T)
 Ans. : $a_n = 1 \text{ m/s}^2, a_t = \sqrt{3} \text{ m/s}^2, \rho = 12 \text{ m}$
11. A particle moves in xy-plane with velocity components $V_x = (8t - 2)$ & $V_y = 2$. If it passes through point $(x,y) = (14, 4)$ when $t=2$ sec, determine the equation of the path traced by the particle. Find also the resultant acceleration at $t=2$ sec.
 Ans. : $x = y^2 - y + 2, a = 8 \text{ m/s}^2 \rightarrow$

12. A particle moves with constant speed of 3m/s along the path $y=3x^2$. Find the acceleration of the particle when $x=0.5\text{m}$. (T)
 Ans. : 1.7m/s^2 , 18.45°



13. A point moves along a path $y=x^2/3$ with a constant speed of 8m/s. What are the x and y components of its velocity when $x=3$? What is the acceleration of the point at this instant?
 Ans. : $V_x=3.76\text{m/s}$, $V_y=7.152\text{m/s}$, $a=3.84\text{m/s}^2$
14. The position vector of a particle is given by $r = 2t^2 .i+4t^{-2} .j$ (m) where t is in seconds. When $t = 1\text{sec}$, determine : (a) the magnitudes of normal and tangential components of acceleration of the particle and (b) the radius of curvature of the path.
 Ans. : $a_t=19.68 \text{ m/s}^2$, $a_n=14.32 \text{ m/s}^2$ 5.586m
15. A skier travels with a constant speed of 6 m/s along the parabolic path $y= x^2 / 20$. Determine his velocity and acceleration at the instant he arrives at A. Neglect the size of the skier in the calculation.
 Ans. : $a_A=1.27 \text{ m/s}^2$ 135° with horizontal
16. A car is traveling along a circular curve having a radius of 50 m. if its speed is 16 m/s and is increasing uniformly at 8 m/s^2 , determine the magnitude of its acceleration at this instant.
 Ans. : 9.50 m/s^2
17. A jet plane flies along the vertical curve having a radius of 800 m. If its speed is uniformly increased from 180 m/s to 230 m/s in 4 s, determine the magnitude of its acceleration at the instant the plane's speed is 200 m/s.
 Ans. : 51.5 m/s^2
18. A point moves along a path $y = 3x^2$ with a constant speed of 8 m/s. What are the x and y components of its velocity when $x= 3\text{m}$. What is the acceleration at this point?